







**#16** Find the values of  $k$  for which the matrix  $A$  is invertible.

$$A = \begin{bmatrix} k & 2 \\ 2 & k \end{bmatrix}$$

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**#35** In each part, find the determinant given that  $A$  is a  $3 \times 3$  matrix for which  $\det(A) = 7$ .

a.  $\det(3A)$

b.  $\det(A^{-1})$

c.  $\det(2A^{-1})$

d.  $\det((2A)^{-1})$

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**Definition:** If  $A$  is any  $n \times n$  matrix and  $C_{ij}$  is the cofactor of  $a_{ij}$ , then the matrix

$\begin{bmatrix} C_{11} & C_{12} & \cdots & C_{1n} \\ C_{21} & C_{22} & \cdots & C_{2n} \\ \vdots & \vdots & & \vdots \\ C_{n1} & C_{n2} & \cdots & C_{nn} \end{bmatrix}$  is called the **matrix of cofactors from A**. The transpose of

this matrix is called the **adjoint of A** and is denoted by  $\text{adj}(A)$ .

**Theorem 2.3.6** Inverse of a Matrix Using Its Adjoint

If  $A$  is an invertible matrix, then  $A^{-1} = \frac{1}{\det(A)} \text{adj}(A)$ .





